

## 3.6 EXERCISES

For the following exercises, given  $y = f(u)$  and  $u = g(x)$ , find  $\frac{dy}{dx}$  by using Leibniz's notation for the chain rule:  $\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$ .

214.  $y = 3u - 6, u = 2x^2$

215.  $y = 6u^3, u = 7x - 4$

216.  $y = \sin u, u = 5x - 1$

217.  $y = \cos u, u = \frac{-x}{8}$

218.  $y = \tan u, u = 9x + 2$

219.  $y = \sqrt{4u + 3}, u = x^2 - 6x$

For each of the following exercises,

a. decompose each function in the form  $y = f(u)$  and  $u = g(x)$ , and

b. find  $\frac{dy}{dx}$  as a function of  $x$ .

220.  $y = (3x - 2)^6$

221.  $y = (3x^2 + 1)^3$

222.  $y = \sin^5(x)$

223.  $y = \left(\frac{x}{7} + \frac{7}{x}\right)^7$

224.  $y = \tan(\sec x)$

225.  $y = \csc(\pi x + 1)$

226.  $y = \cot^2 x$

227.  $y = -6\sin^{-3} x$

For the following exercises, find  $\frac{dy}{dx}$  for each function.

228.  $y = (3x^2 + 3x - 1)^4$

229.  $y = (5 - 2x)^{-2}$

230.  $y = \cos^3(\pi x)$

231.  $y = (2x^3 - x^2 + 6x + 1)^3$

232.  $y = \frac{1}{\sin^2(x)}$

233.  $y = (\tan x + \sin x)^{-3}$

234.  $y = x^2 \cos^4 x$

235.  $y = \sin(\cos 7x)$

236.  $y = \sqrt{6 + \sec \pi x^2}$

237.  $y = \cot^3(4x + 1)$

238. Let  $y = [f(x)]^3$  and suppose that  $f'(1) = 4$  and  $\frac{dy}{dx} = 10$  for  $x = 1$ . Find  $f(1)$ .

239. Let  $y = (f(x) + 5x^2)^4$  and suppose that  $f(-1) = -4$  and  $\frac{dy}{dx} = 3$  when  $x = -1$ . Find  $f'(-1)$ .

240. Let  $y = (f(u) + 3x)^2$  and  $u = x^3 - 2x$ . If  $f(4) = 6$  and  $\frac{dy}{dx} = 18$  when  $x = 2$ , find  $f'(4)$ .

241. **[T]** Find the equation of the tangent line to  $y = -\sin\left(\frac{x}{2}\right)$  at the origin. Use a calculator to graph the function and the tangent line together.

242. **[T]** Find the equation of the tangent line to  $y = \left(3x + \frac{1}{x}\right)^2$  at the point  $(1, 16)$ . Use a calculator to graph the function and the tangent line together.

243. Find the  $x$ -coordinates at which the tangent line to  $y = \left(x - \frac{6}{x}\right)^8$  is horizontal.

244. **[T]** Find an equation of the line that is normal to  $g(\theta) = \sin^2(\pi\theta)$  at the point  $\left(\frac{1}{4}, \frac{1}{2}\right)$ . Use a calculator to graph the function and the normal line together.

For the following exercises, use the information in the following table to find  $h'(a)$  at the given value for  $a$ .