

x	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
0	2	5	0	2
1	1	-2	3	0
2	4	4	1	-1
3	3	-3	2	3

245. $h(x) = f(g(x)); a = 0$

246. $h(x) = g(f(x)); a = 0$

247. $h(x) = (x^4 + g(x))^{-2}; a = 1$

248. $h(x) = \left(\frac{f(x)}{g(x)}\right)^2; a = 3$

249. $h(x) = f(x + f(x)); a = 1$

250. $h(x) = (1 + g(x))^3; a = 2$

251. $h(x) = g(2 + f(x^2)); a = 1$

252. $h(x) = f(g(\sin x)); a = 0$

253. [T] The position function of a freight train is given by $s(t) = 100(t + 1)^{-2}$, with s in meters and t in seconds.

At time $t = 6$ s, find the train's

- velocity and
- acceleration.
- Using a. and b. is the train speeding up or slowing down?

254. [T] A mass hanging from a vertical spring is in simple harmonic motion as given by the following position function, where t is measured in seconds and s is in inches: $s(t) = -3 \cos\left(\pi t + \frac{\pi}{4}\right)$.

- Determine the position of the spring at $t = 1.5$ s.
- Find the velocity of the spring at $t = 1.5$ s.

255. [T] The total cost to produce x boxes of Thin Mint Girl Scout cookies is C dollars, where $C = 0.0001x^3 - 0.02x^2 + 3x + 300$. In t weeks production is estimated to be $x = 1600 + 100t$ boxes.

- Find the marginal cost $C'(x)$.
- Use Leibniz's notation for the chain rule, $\frac{dC}{dt} = \frac{dC}{dx} \cdot \frac{dx}{dt}$, to find the rate with respect to time t that the cost is changing.
- Use b. to determine how fast costs are increasing when $t = 2$ weeks. Include units with the answer.

256. [T] The formula for the area of a circle is $A = \pi r^2$, where r is the radius of the circle. Suppose a circle is expanding, meaning that both the area A and the radius r (in inches) are expanding.

- Suppose $r = 2 - \frac{100}{(t + 7)^2}$ where t is time in seconds. Use the chain rule $\frac{dA}{dt} = \frac{dA}{dr} \cdot \frac{dr}{dt}$ to find the rate at which the area is expanding.
- Use a. to find the rate at which the area is expanding at $t = 4$ s.

257. [T] The formula for the volume of a sphere is $S = \frac{4}{3}\pi r^3$, where r (in feet) is the radius of the sphere.

Suppose a spherical snowball is melting in the sun.

- Suppose $r = \frac{1}{(t + 1)^2} - \frac{1}{12}$ where t is time in minutes. Use the chain rule $\frac{dS}{dt} = \frac{dS}{dr} \cdot \frac{dr}{dt}$ to find the rate at which the snowball is melting.
- Use a. to find the rate at which the volume is changing at $t = 1$ min.

258. [T] The daily temperature in degrees Fahrenheit of Phoenix in the summer can be modeled by the function $T(x) = 94 - 10 \cos\left[\frac{\pi}{12}(x - 2)\right]$, where x is hours after midnight. Find the rate at which the temperature is changing at 4 p.m.

259. [T] The depth (in feet) of water at a dock changes with the rise and fall of tides. The depth is modeled by the function $D(t) = 5 \sin\left(\frac{\pi}{6}t - \frac{7\pi}{6}\right) + 8$, where t is the number of hours after midnight. Find the rate at which the depth is changing at 6 a.m.