550. A rocket is launched into space; its kinetic energy is given by $K(t) = \left(\frac{1}{2}\right)m(t)v(t)^2$, where *K* is the kinetic energy in joules, *m* is the mass of the rocket in kilograms, and *v* is the velocity of the rocket in meters/second. Assume the velocity is increasing at a rate of 15 m/sec² and the mass is decreasing at a rate of 10 kg/sec because the fuel is being burned. At what rate is the rocket's kinetic energy changing when the mass is 2000 kg and the velocity is 5000 m/sec? Give your answer in mega-Joules (MJ), which is equivalent to 10^6 J.

551. The famous Regiomontanus' problem for angle maximization was proposed during the 15 th century. A painting hangs on a wall with the bottom of the painting a distance *a* feet above eye level, and the top *b* feet above eye level. What distance *x* (in feet) from the wall should the viewer stand to maximize the angle subtended by the painting, θ ?



552. An airline sells tickets from Tokyo to Detroit for \$1200. There are 500 seats available and a typical flight books 350 seats. For every \$10 decrease in price, the airline observes an additional five seats sold. What should the fare be to maximize profit? How many passengers would be onboard?