

5.6 Integrals Involving Exponential and Logarithmic Functions

- Exponential and logarithmic functions arise in many real-world applications, especially those involving growth and decay.
- Substitution is often used to evaluate integrals involving exponential functions or logarithms.

5.7 Integrals Resulting in Inverse Trigonometric Functions

- Formulas for derivatives of inverse trigonometric functions developed in **Derivatives of Exponential and Logarithmic Functions** lead directly to integration formulas involving inverse trigonometric functions.
- Use the formulas listed in the rule on integration formulas resulting in inverse trigonometric functions to match up the correct format and make alterations as necessary to solve the problem.
- Substitution is often required to put the integrand in the correct form.

CHAPTER 5 REVIEW EXERCISES

True or False. Justify your answer with a proof or a counterexample. Assume all functions f and g are continuous over their domains.

439. If $f(x) > 0$, $f'(x) > 0$ for all x , then the right-hand rule underestimates the integral $\int_a^b f(x)$. Use a graph to justify your answer.

440. $\int_a^b f(x)^2 dx = \int_a^b f(x) dx \int_a^b f(x) dx$

441. If $f(x) \leq g(x)$ for all $x \in [a, b]$, then $\int_a^b f(x) \leq \int_a^b g(x)$.

442. All continuous functions have an antiderivative.

Evaluate the Riemann sums L_4 and R_4 for the following functions over the specified interval. Compare your answer with the exact answer, when possible, or use a calculator to determine the answer.

443. $y = 3x^2 - 2x + 1$ over $[-1, 1]$

444. $y = \ln(x^2 + 1)$ over $[0, e]$

445. $y = x^2 \sin x$ over $[0, \pi]$

446. $y = \sqrt{x} + \frac{1}{x}$ over $[1, 4]$

Evaluate the following integrals.

447. $\int_{-1}^1 (x^3 - 2x^2 + 4x) dx$

448. $\int_0^4 \frac{3t}{\sqrt{1+6t^2}} dt$

449. $\int_{\pi/3}^{\pi/2} 2 \sec(2\theta) \tan(2\theta) d\theta$

450. $\int_0^{\pi/4} e^{\cos^2 x} \sin x \cos x dx$

Find the antiderivative.

451. $\int \frac{dx}{(x+4)^3}$

452. $\int x \ln(x^2) dx$

453. $\int \frac{4x^2}{\sqrt{1-x^6}} dx$

454. $\int \frac{e^{2x}}{1+e^{4x}} dx$

Find the derivative.

455. $\frac{d}{dt} \int_0^t \frac{\sin x}{\sqrt{1+x^2}} dx$