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Due Monday, September 11.

1. Consider the DFA shown below.
(a) What are the sets $Q, \Sigma$, and $F$ in the formal description $(Q, \Sigma, \delta, q, F)$ of this machine?
(b) What sequence of states does the machine go through on the input aabbaa? Does the machine accept aabbaa?

2. Design a DFA that outputs 1 if and only if the input length is divisible by 3 . Draw a state diagram for you answer.
3. Design a DFA that outputs 1 if and only if the input begins with 01 and ends with 01 . Draw a state diagram for your answer.
4. Construct an NFA with three states that accepts a string in $\{0,1\}^{*}$ iff it ends in 00 .
5. Find a DFA that is equivalent to the NFA shown below.

6. Consider a DFA with states $Q=\{0,1,2\}$, alphabet $\Sigma=\{0,1\}$, initial state $q_{0}=0$, and accepting states $F=\{0,1\}$. The transition function is shown in the table below. Write a computer program that takes a string in $\Sigma^{*}$ as input and prints each state the DFA enters as it goes through the input string. Your program should also return 1 if the DFA accepts the string, otherwise return 0 .

|  | $\sigma$ | 0 |
| :---: | :--- | :--- |
| 0 | 1 |  |
| 1 | 1 | 1 |
| 2 | 0 | 2 |
|  | 0 | 0 |

