Homework 8 - Math 142

Name: _____

1. Compute
$$\lim_{x \to 2} \frac{x^2 + 3x - 10}{x - 2}$$

2. Compute $\lim_{x \to \pi} \frac{x - \pi}{\sin x}$.

3. Find
$$\lim_{x \to 0^+} \left(\frac{12}{x} - \frac{5}{x^2}\right)$$
.

4. Find $\lim_{x\to\infty} x^{1/x}$. Hint: Let $A = \lim_{x\to\infty} x^{1/x}$ and take the natural log of both sides.

5. Which function grows faster as $x \to \infty$, $f(x) = \ln(x^2)$ or $g(x) = \sqrt{x}$? Use L'Hospital's rule to find out.

6. Find
$$\int_0^\infty x^2 e^{-2x} \, dx.$$

7. Show that each of the following integrals diverge by finding a smaller (simpler) integral that diverges.

(a)
$$\int_0^1 \frac{e^x}{x^2} dx$$

(b)
$$\int_{e}^{\infty} \sqrt{\ln x} \, dx$$

8. For each of the following, find a larger integral that converges.

(a)
$$\int_0^\infty e^{-x} \sin^2 x \, dx$$

(b)
$$\int_{1}^{\infty} \frac{\sqrt{x}}{1+x^2} \, dx$$

9. Determine whether the integral $\int_{2}^{\infty} \sqrt{\frac{\sqrt{x+3}}{x-1}} dx$ converges or diverges by finding a simpler integral to compare it with. Clearly explain how your comparison works.