

An Example of Inference

Math 121 - Workshop

The herbal supplement Garcinia Cambogia is advocated by Dr. Mehmet Oz (a celebrity doctor) as an effective weight loss aid. A 1998 study of 135 people found that it was not significantly better than a placebo. Here is the abstract from the study.

A total of 135 subjects were randomized to either active hydroxycitric acid [The active ingredient in G. Cambogia] ($n = 66$) or placebo ($n = 69$); 42 (64%) in the active hydroxycitric acid group and 42 (61%) in the placebo group completed 12 weeks of treatment. Patients in both groups lost a significant amount of weight during the 12-week treatment period; however, between-group weight loss differences were not statistically significant (mean [SD], 3.2 [3.3] kg vs 4.1 [3.9] kg; $P = 0.14$).

This table summarizes the data described above:

Group	N	\bar{x}	s
Treatment	42	4.1	3.9
Control	42	3.2	3.3

1. This is an example of a randomized controlled experiment. Why is it important to use a randomized experiment in this situation instead of an observational study?
2. What are the explanatory and response variables?
3. According to the study, “patients in both groups lost a significant amount of weight”. It is a little surprising that patients in the placebo group lost a significant amount of weight! Do a one-sample t-test to see if this is correct. What are the hypotheses? What is the t-value, and what is the p-value? You can use the interactive formula sheet and t-distribution app to speed up your calculations.

- While both groups lost a significant amount of weight, the important question is whether the people taking Garcinia Cambogia lost significantly more weight than people taking a placebo. Do a two-sample t-test to find out. What are the correct hypotheses, what is the t-value, and what is the p-value? Do you get a p-value that is close to what the researchers reported ($P = 0.14$)?
- According to the researchers, the effect of Garcinia Cambogia is not statistically significant. Which of the following options best describes what this means?
 - Garcinia Cambogia definitely does not increase weight loss.
 - Garcinia Cambogia is no different than a placebo, on average.
 - The observed difference between the Garcinia Cambogia group and the placebo group might have been random chance.
 - The observed difference between the Garcinia Cambogia group and the placebo group was not very large.
- One big advantage of confidence intervals over hypothesis tests is that confidence intervals let you estimate the **effect size** of a treatment. Make a 95% confidence interval for the difference in mean weight loss between the two groups.