

1. Suppose that  $x_1, x_2, \dots, x_n$  are real numbers. Prove that

$$|x_1 + x_2 + \dots + x_n| \leq |x_1| + |x_2| + \dots + |x_n|.$$

(Hint: Use induction.)

2. Let  $y > 0$ . Prove that there exists a *unique*  $n \in \mathbb{N}$  such that  $n - 1 \leq y < n$ .  
(Hint: You need to prove existence and uniqueness separately.)

3. Let  $S \subseteq \mathbb{R}$  and  $x \in \mathbb{R}$ . Prove that one and only one of the following conditions holds:

- (a)  $x \in \text{int } S$
- (b)  $x \in \text{int } (\mathbb{R} \setminus S)$
- (c)  $x \in \text{bd } S = \text{bd } (\mathbb{R} \setminus S)$