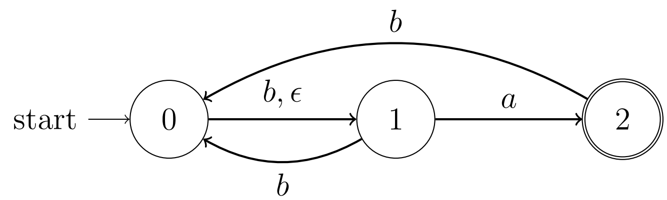
Homework 4 - Computer Science 461 **Name:** ______________________

Due Monday, September 18.

1. Convert the following NFA to a DFA. Use the method we discussed in class, where the states of the DFA correspond to subsets of the states of the original NFA. Hint: *After removing states in the DFA that you can never reach, you should only need a small number of states, one of which corresponds to the empty set.*



2. Let $\Sigma = \{0,1\}$. Write a one-sentence description the languages defined by the following regular expressions. For example: Σ^*1 would be any binary string that ends with a 1.
   (a) $(\Sigma\Sigma)^*$.

   (b) $\Sigma^*01\Sigma^*$.

   (c) $(0\Sigma^*0)|(1\Sigma^*1)$.

3. Find a regular expression that matches each of the following languages. In all cases, the alphabet is $\Sigma = \{0,1\}$.
   (a) $\{w \in \Sigma^* : w$ contains at least three 1's.$\}$

   (b) $\{w \in \Sigma^* : w$ contains at least two 1's and exactly one 0.$\}$

4. Let Σ be the regular English alphabet $\{a, b, c, \ldots, z\}$. Write a regular expression that matches all strings that contain at least two vowels (i.e., a,e,i,o,u).

5. Prove that if $L \subset \Sigma^*$ is a regular language, then complement $\Sigma^* \backslash L$ is also a regular language. Hint: *If there is a DFA $M = (Q, \Sigma, \delta, q, F)$ that recognizes L, describe a different DFA that recognizes the complement.*

6. Let $L = \{w \in \Sigma^* :$ the length of w is a power of $2\}$. Use the pumping lemma to prove that L is not a regular language.