

# Divisibility

## Lecture 4

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# Outline

- 1 Divisibility
- 2 L<sup>A</sup>T<sub>E</sub>X
- 3 Divisibility Conjectures

1 Divisibility

2 L<sup>A</sup>T<sub>E</sub>X

3 Divisibility Conjectures

## Definition (Divisibility)

Let  $n$  and  $m$  be integers. Then  $n$  **divides**  $m$ , written  $n \mid m$ , if  $n \neq 0$  and there is an integer  $k$  such that  $nk = m$ .

# Outline

1 Divisibility

2  $\text{L}^{\text{A}}\text{T}_{\text{E}}\text{X}$

3 Divisibility Conjectures

L<sup>A</sup>T<sub>E</sub>X

- Use `\mid` to create the “divides” sign  $|$ .
- Use `\nmid` to create the “does not divide” sign  $\nmid$ .

Examples:

- $3 \mid 6$
- $4 \nmid 6$

# Outline

1 Divisibility

2 L<sup>A</sup>T<sub>E</sub>X

**3 Divisibility Conjectures**

# Conjecture

## Problem

*Prove or disprove: For any integer  $n$ ,  $n \mid 0$ .*



# Conjecture

## Problem

*Prove or disprove: For any nonzero integer  $n$ ,  $n \mid 0$ .*

# Conjecture

## Problem

*Prove or disprove: For any integer  $n$ ,  $1 \mid n$ .*

# Conjecture

## Problem

*Prove or disprove: For any integer  $a$ , if  $a \mid 1$ , then  $a = 1$  or  $a = -1$ .*

# Conjecture

## Problem

*Prove or disprove: For any integers  $a$  and  $b$ , if  $a \mid b$  and  $b \mid a$ , then  $a = b$  or  $a = -b$ .*

# Conjecture

## Problem

*Prove or disprove: For any integers  $a$ ,  $b$ , and  $c$ , if  $a \mid b$  and  $a \mid b + c$ , then  $a \mid c$ .*

# Conjecture

## Problem

*Prove or disprove: For any integers  $a$ ,  $b$ , and  $c$ , if  $a \nmid b$  and  $a \nmid c$ , then  $a \nmid b + c$ .*

# Conjecture

## Problem

*Prove or disprove: For any integers  $a$ ,  $b$ , and  $c$ , if  $a \mid b$  and  $a \nmid c$ , then  $a \nmid b + c$ .*

# Conjecture

## Problem

*Prove or disprove: For any integers  $a$ ,  $b$ , and  $c$ , if  $a \mid c$  and  $b \mid c$ , then  $a + b \mid c$ .*