

Boxplots

Robb T.
Koether

Boxplots

TI-83 Boxplots

Modified Boxplots

TI-83 Modified
Boxplots

Assignment

Answers to
Even-
numbered
Exercises

Boxplots

Lecture 17

Section 5.3.3

Robb T. Koether

Hampden-Sydney College

Wed, Sep 23, 2009

Outline

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Definition (Boxplot)

A **boxplot** is a graphical display of a five-number summary.

- The interquartile range is represented by a rectangle over a vertical scale.
- The median is represented by a vertical line through the rectangle.
- The maximum and minimum are represented by “tails” or “whiskers” attached to the ends of the rectangle.

Example

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Example (Boxplot)

- Draw a boxplot of the sample

5, 20, 30, 45, 60, 80, 100, 140, 150, 200, 240.

Example

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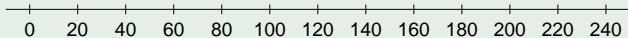
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Example (Boxplot)



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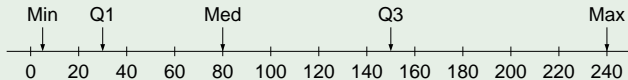
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Example (Boxplot)



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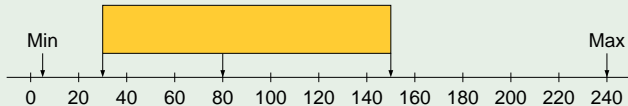
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Example (Boxplot)



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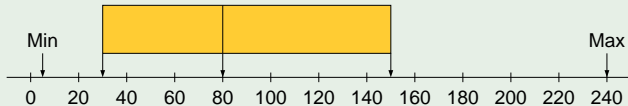
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Example (Boxplot)



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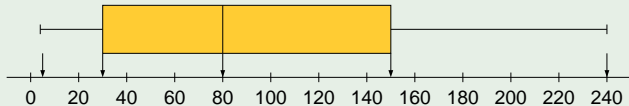
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Example (Boxplot)



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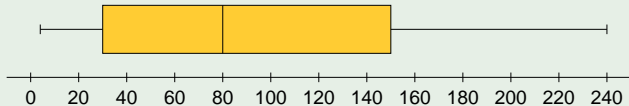
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Example (Boxplot)



Boxplots and Shape

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- What would a boxplot for a uniform distribution look like?
- What would a boxplot for a symmetric distribution look like?
- What would a boxplot for a right-skewed distribution look like?

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TI-83 Boxplots

- Press `STAT PLOT`.
- Select `Plot1`
- Turn `Plot1` On.
- Under `Type`, select the boxplot icon (2nd row, 2nd icon).
- Specify list `L1`.
- Press `ZOOM`.
- Select `ZoomStat (#9)` and press `ENTER` (or press `9`).

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TI-83 Boxplots

- To get the five-number summary from the boxplot,
 - Press `TRACE`.
 - Use the arrow keys to see the values of the minimum, Q_1 , the median, Q_3 , and the maximum.

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Example (TI-83 Boxplots)

- Use the TI-83 to draw a boxplot of the rainfall data.

15.09	2.82	24.18	0.20	15.60	22.04
7.44	5.16	9.14	37.36	10.19	2.16
17.50	28.12	11.23	8.66	7.24	6.50
4.88	13.08	4.01	11.28	1.96	12.09
2.92	7.67	4.39	6.60	6.50	25.43

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Definition (Outlier)

An **outlier** is any value that is more than 1.5 IQR below Q_1 or more than 1.5 IQR above Q_3 .

Definition (Extreme outlier)

An **extreme outlier** is any value that is more than 3 IQR below Q_1 or more than 3 IQR above Q_3 .

Definition (Modified boxplot)

A **modified boxplot** is a boxplot in which the outliers (and extreme outliers) are indicated by separate dots.

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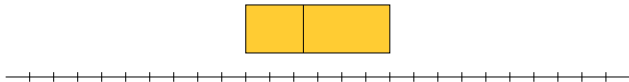
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- To draw a modified boxplot,
 - Draw the box part of the boxplot as usual.
 - Compute $\text{STEP} = 1.5 \times \text{IQR}$.
 - The inner fences are at $Q_1 - \text{STEP}$ and $Q_3 + \text{STEP}$.



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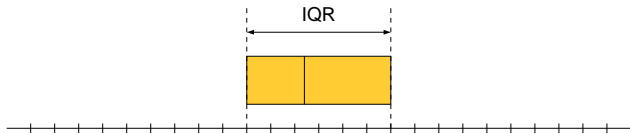
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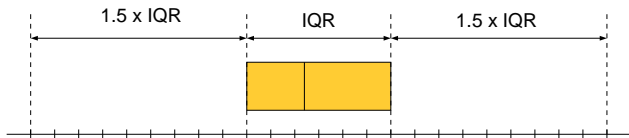
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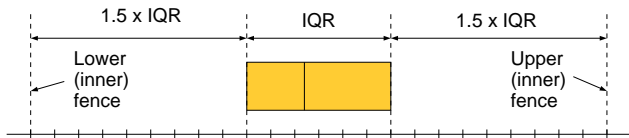
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- Extend the whiskers from the box to the smallest and largest values that are within the inner fences.
- Any values that are outside the inner fences should be drawn as individual dots.
- These dots represent outliers.

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Practice

- Draw a modified boxplot of the sample

9, 13, 38, 40, 42, 43, 46, 47, 49, 53, 55, 60, 84.

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TI-83 Modified Boxplots

- Follow the same steps as for a regular boxplot, but for the `Type`, select the modified-boxplot icon, the first icon in the second row. It looks like a boxplot with a couple of extra dots.

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Example

TI-83 Modified Boxplots

- Use the TI-83 to draw a modified boxplot of the rainfall data.

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9, 13, 38, 40, 42, 43, 46, 47, 49, 53, 55, 60, 84.

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- For an example of modified boxplots, see [DePaul University's web page on retention.](#)

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Homework

- Read Section 5.3.3, pages 315 - 325.
- Let's Do It! 5.8, 5.9, 5.10, 5.11.
- Page 333, exercises 12, 13, 15, 19.

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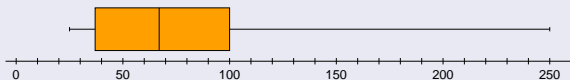
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Page 333, Exercise 12

5.12 (a)



(b) It is more than 50%, but not more than 75%.

(c) \$37,000